This exam has 9 questions, for a total of 100 points.

1. [5 points] What is the output of the following Python program,

```python
x = input()
print x + input() % input(), False, True
```

given the input

-2
-1
4

Solution:

1 False True

2. [15 points] Draw a parse tree and an abstract syntax tree (AST) for the program in the previous question, given the grammar below and the usual precedence rules for Python. The AST should match what the Python compiler module would produce.

Grammar:

expression ::= identifier | integer | "True" | "False" |
expression "%" expression | expression "+" expression |
"input" "(" ")"
expression_list ::= expression | expression \, expression_list
statement ::= identifier "=" expression | "print" expression_list
stmt_list ::= statement | statement stmt_list

Solution:

Parse tree:
3. **5 points** Write down the definition of the `pyobj` struct used to implement the $P_1$ language, which contains normal integers, floats, and Booleans

**Solution:**

```c
enum type_tag { INT, FLOAT, BOOL };  
struct pyobj_struct  
{  
  enum type_tag tag;  
  union  
  {  
    int i;   /* int */  
    double f; /* float */  
    short b;  /* bool */  
  } u;  
};  
typedef struct pyobj_struct pyobj;
```
4. **10 points** Write down the implementation of a C function for dividing two \texttt{pyobj} for the \textit{P}$_1$ language.

Solution:

```c
pyobj divide(pyobj a, pyobj b)
{
    if(b.type==BOOL) {
        if(b.v.b==0) {
            error("can't divide by zero");
        } else if(a.type==BOOL) {
            return int_to_pyobj(a.v.b);
        } else {
            return a;
        }
    } else {
        pyobj res;
        if((a.type==FLOAT) || (b.type==FLOAT)) {
            double l, r;
            l = pyobj_to_float(a);
            r = pyobj_to_float(b);
            res.type = FLOAT;
            if((r==0.0) || (r==-0.0)) { error("can't divide by zero"); }
            res.v.f = l/r;
        } else {
            int l, r;
            l = pyobj_to_int(a);
            r = pyobj_to_int(b);
            res.type = INT;
            if(r==0) { error("can't divide by zero"); }
            res.v.i = (int)floor(((double)l)/((double)r));
        }
        return res;
    }
}
```


5. **15 points** Convert the following Python program to Static Single-Assignment (SSA) form.

```python
x = 0
y = 0

def f(z):
    while x < y:
        y = y + 1
        z = x - 1
        if x < z:
            y = y + 1
        else:
            y = z
    return x + y + z

def f(z):
    return z
f(x)
```

**Solution:**

```python
x_0 = 0
y_0 = 0

def f_0(z_0):
    while True:
        y_1 = φ(uninitialized, y_5)
        z_2 = φ(z_0, z_1)
        if x_0 < y_1:
            y_2 = y_1 + 1
            z_1 = x_0 - 1
            if x_0 < z_1:
                y_3 = y_2 + 1
            else:
                y_4 = z_1
                y_5 = φ(y_3, y_4)
        else:
            break
    return x_0 + y_1 + z_2

def f_1(z_0):
    return z_0
f_1(x_0)
```
6. **20 points** Perform iterative type analysis and type specialization on the following program and write down the C code that your compiler would generate. You do not need to write down the implementations of the C structs or run-time functions that you use, but you do need to write down the function declarations (e.g., `pyobj add_pyobj(pyobj,pyobj);`).

```c
z = 0
y = 1 if input() else 2
x = y or 1
while z < y:
    z = z + x
    y = y - 0.5
print z
```

**Solution:**

```c
int main() {
    int z_0;
    int z_1;
    int z_2;
    int x_0;
    pyobj y_2;
    pyobj y_1;
    int y_0;
    z_0 = 0;
    y_0 = (is_true(input()) ? 1:2);
    x_0 = ({ int tmp0_0 = y_0; (tmp0_0 ? tmp0_0:1);});
    y_1 = make_int(y_0);
    z_1 = z_0;
    while (is_true(({ int tmp1_0 = z_1; less(make_int(tmp1_0), y_1);}))) {
        z_2 = add_int(z_1, x_0);
        y_2 = sub(y_1, make_float(0.5));
        y_1 = y_2;
        z_1 = z_2;
    }
    print_any(make_int(z_1));printf("\n");
    return 0;
}
```
7. **5 points** What is the output of the following Python program?

```python
i = 0
a = {}
while i < 3:
    a[i] = lambda: i
    i = i + 1
j = 0
while j < 3:
    print a[j]()
    j = j + 1
```

**Solution:**

3
3
3
8. **20 points** Perform closure conversion on the program from the previous question, translating it to an equivalent Python program where no function has free variables.

**Solution:**

```python
def make_closure(f, fvs):
    return [f, fvs]
def get_function(closure):
    return closure[0]
def get_fvs(closure):
    return closure[1]

def anon_0(fvs):
    i = fvs[0]
    return i[0]

i = [False]
i[0] = 0
a = {}
while i[0] < 3:
    a[i[0]] = make_closure(anon_0, [i])
    i[0] = i[0] + 1
j = 0
while j < 3:
    tmp = a[j]
    print get_function(tmp)(get_fvs(tmp))
    j = j + 1
```
9. **5 points** What is the output of the following Python program?

```python
true = lambda x: lambda y: x()
false = lambda x: lambda y: y()

def equal(a, b):
    return true if a == b else false

def f(n):
    return equal(n, 0) \ 
    (lambda: 0) \ 
    (lambda: equal(n,1) \ 
    (lambda: 1) \ 
    (lambda: f(n - 1) + f(n - 2)))

print f(6)
```

**Solution:**

8