
Example 2.11 Calculate the electron and hole densities in an n-type silicon wafer ($N_d = 10^{17} \text{ cm}^{-3}$) illuminated uniformly with 10 mW/cm^2 of red light ($E_{ph} = 1.8 \text{ eV}$). The absorption coefficient of red light in silicon is 10^{-3} cm^{-1} . The minority carrier lifetime is $10 \mu\text{s}$.

Solution The generation rate of electrons and holes equals:

$$G_n = G_p = \alpha \frac{P_{opt}}{E_{ph} A} = 10^{-3} \frac{10^{-2}}{1.8 \times 1.6 \times 10^{-19}} = 3.5 \times 10^{13} \text{ cm}^{-3} \text{ s}^{-1}$$

where the photon energy was converted into Joules. The excess carrier densities are then obtained from:

$$\Delta n = \Delta p = \tau_p G_p = 10 \times 10^{-6} \times 3.5 \times 10^{13} = 3.5 \times 10^8 \text{ cm}^{-3}$$

So that the electron and hole densities equal:

$$n = n_o + \Delta n = 10^{17} + 3.5 \times 10^8 = 10^{17} \text{ cm}^{-3}$$

$$p = \frac{n_i^2}{n_o} + \Delta p = \frac{(10^{10})^2}{10^{17}} + 3.5 \times 10^8 = 3.5 \times 10^8 \text{ cm}^{-3}$$
