

Problems

1. Consider an aluminum-SiO₂-silicon MOS capacitor ($F_M = 4.1$ V, $\epsilon_{ox}/\epsilon_0 = 3.9$, $\chi = 4.05$ V and $N_a = 10^{17}$ cm⁻³) MOS capacitor with $t_{ox} = 5$ nm.
 - a) Calculate the flatband voltage and threshold voltage.
 - b) Repeat for an n-type silicon substrate with $N_d = 10^{16}$ cm⁻³.
 - c) Repeat with a surface charge of 10^{-7} C/cm²
 - d) Repeat with a charge density in the oxide of 10^{-1} C/cm³
2. A high-frequency capacitance voltage measurement of a silicon MOS structure was fitted by the following expression:

$$C(V_G) = 6 \text{ pF} + 12 \text{ pF} / (1 + \exp(V_G))$$

- a) Calculate the oxide capacitance per unit area and the oxide thickness. The area of the capacitor is 100 x 100 micron and the relative dielectric constant equals 3.9.
 - b) From the minimum capacitance, calculate the maximum depletion layer width and the substrate doping density.
 - c) Calculate the bulk potential.
 - d) Calculate the flatband capacitance and the flatband voltage.
 - e) Calculate the threshold voltage.
3. An MOS capacitor with an oxide thickness of 20 nm has an oxide capacitance, which is three times larger than the minimum high-frequency capacitance in inversion. Find the substrate doping density.
 4. A CMOS gate requires n-type and p-type MOS capacitors with a threshold voltage of 2 and -2 Volt respectively. If the gate oxide is 50 nm what are the required substrate doping densities? Assume the gate electrode is aluminum. Repeat for a p⁺ poly-silicon gate.
 5. Consider a p-MOS capacitor (with an n-type substrate) and with an aluminum gate. Find the doping density for which the threshold voltage is 3 times larger than the flat band voltage. $t_{ox} = 25$ nm. Repeat for a capacitor with 10^{11} cm⁻² electronic charges at the oxide-semiconductor interface.
 6. A silicon p-MOS capacitor ($N_d = 4 \times 10^{16}$ cm⁻³, $t_{ox} = 40$ nm) is biased halfway between the flatband and threshold voltage. Calculate the applied voltage and the corresponding capacitance