Tomographic reconstruction of weak, replicated index structures embedded in a volume

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Abstract: Measurements of weak, embedded index structures are important for material characterization of photopolymers, glass and other optical materials as well as for characterization of fabricated structures such as waveguides. We demonstrate an optical diffraction tomography system capable of measuring deeply-buried, weak, fabricated index structures written in a homogeneous volume. High-fidelity cross sections of these weak index structures are constructed by replicating the structure to be measured to form a diffraction grating. The coherent addition of scattering from each of these objects increases the sensitivity of the imaging system. Measurements are made in the far field, without the use of lenses, eliminating phase aberration errors through thick volumes.

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References and links

1. Introduction

Quantitative, high-resolution images of weak index structures are important for a wide variety of applications. Accurate measurements of index changes in volume photopolymers are necessary for storage applications such as volume holographic storage and microholographic volume data storage [1–7]. Waveguides can also be written in photopolymers by mask lithography [8], using light from an embedded fiber to self-write a waveguide [9,10], or three-dimensional (3D) direct-write lithography [11]. Femtosecond writing in glass is also used to create embedded 3D waveguides and integrated optical circuits [12–14]. Quantitative measurements of these index structures written in photopolymers or glass are essential for design verification and development of materials response models. In this paper, we demonstrate an optical diffraction tomography system capable of quantitative imaging of weak index structures written in a 3D volume. This is accomplished by making many identical, equally-spaced copies of the object to be measured in order to increase the sensitivity of the imaging system. Many fabrication techniques, such as those described above, are capable of replicating many copies of the objects to be imaged. As we demonstrate in this paper, this allows for imaging weak index structures with a higher signal to noise ratio than traditional tomography.

Small or weak variations in the index can be very difficult to measure and the thickness of the samples makes imaging even more challenging. The total phase delay across small features can be much less than a single wavelength for a structure embedded millimeters deep in a glass or polymer sample. Differential Interference Contrast (DIC) microscopy is one technique for imaging these structures qualitatively and recent work has shown quantitative measurements of thin objects [15–17]. However, high-power objectives accumulate significant spherical aberrations when imaging through thick objects and have limited working distances. The objectives can be corrected for certain depths but cannot usually...
image accurately over a wide range of depths, such as the 1 mm depth scanning required for many applications. Confocal scanning microscopy has excellent depth sectioning [18], but confocal reflection systems are not sensitive to the spatial frequencies of index structures written by a focused beam unless the numerical aperture (NA) of the confocal microscope is significantly higher than that of the NA of the writing lens [19]. Confocal transmission microscopy, on the other hand, is sensitive to objects with lower spatial frequencies, but is challenging to implement due to deflection and aberration of the transmitted spot [20,21]. All of the above techniques also have the same problem of accumulating significant spherical aberrations through very thick objects, which limits the working distance of the imaging system. Thick index objects can be sliced thinly in order to be imaged using one of these phase microscopy techniques; however, this may damage the object to be imaged.

Optical diffraction tomography solves many of these problems but has several limitations of its own. Diffraction tomography works by measuring the fields diffracted from an object at a number of incident probe beam angles and backpropagating the fields to reconstruct the scattering object. A collimated probe beam can be used, eliminating the need for high NA lenses and therefore eliminating phase aberration errors in the image. Also, by measuring the scattered field at a number of incident angles, the object is imaged in both the transverse and depth dimensions, allowing quantitative imaging of thick objects. Normally, diffraction tomography requires information about the phase of the scattered fields. This requirement significantly complicates both the experimental set up and the numerical reconstruction. Also, an object with a phase delay of much less than one wavelength diffracts light with an efficiency that is typically lower than the scattering background. Therefore, it is difficult to distinguish the signal from the noise. The tomography system reported here overcomes these two difficulties. First, for symmetric objects, phase information is not necessary for the reconstruction. The low signal-to-noise problem is addressed by duplicating the object of interest on a regular grid so that the scatter from each object adds coherently to the others, giving a stronger signal for the reconstruction. This method of duplicating the object of interest and reconstructing the object from discrete samples in the far field is similar to that used for x-ray diffraction measurements of crystals [22].

In Sec. 2, we review the fundamentals of optical diffraction tomography and the modifications made to the reconstruction algorithm for imaging diffraction gratings without phase. We then describe a 3D lithography system for fabricating a grid of identical weak, index structures with the required symmetry in Sec. 3. Details of the tomography system and the results and validation are presented in Sec. 4.

2. Optical diffraction tomography: theory

Optical diffraction tomography is used to reconstruct weak 3D index perturbations from a series of two-dimensional (2D) diffracted field measurements taken over a range of probe beam incident angles [23,24]. In the Born approximation, where the perturbation is small enough that the probe beam is essentially undepleted, the Fourier transform of the index perturbation is directly related to the Fourier transform of the scattered near field. Backpropagation of the scattered fields is accomplished by inverting the forward scattering problem. For many applications, the index perturbation is constant or slowly varying in one dimension and so the following derivation is concerned with imaging two dimensional cross sections of the index perturbation.

The problem of scattering off of inhomogeneous media is complex in full vector form, but a number of approximations can be made to simplify the problem for practical applications. It is common to assume that the scattering object varies slowly in space, i.e., it does not change significantly over distances on the order of the wavelength of the incident light. This simplification uncouples the different components of the electric field in the wave equation and simplifies the problem to the scalar case, which can be expressed in terms of the index of refraction, $n$, as
\[
\left( \nabla^2 + k_0^2 n_0^2 \right) E(x, z) = k_0^2 n_0^2 \left( 1 - \frac{n^2(x, z)}{n_0^2} \right) E(x, z), \tag{1}
\]

where \( E(x, z) \) is the electric field of the probe beam, \( n(x, z) = n_0 + \delta n(x, z) \) is the sum of the background index and the index perturbation, and \( k_0 = 2\pi/n_0 \) is the wave number in free space. This simplification limits the applicable resolution of the tomography system to the order of a wavelength of the probe beam.

In the Born approximation, where the scattering is weak, the expression in the parentheses on the right side of Eq. (1) can be approximated by

\[
1 - \frac{n^2(x, z)}{n_0^2} \approx -\frac{2\delta n(x, z)}{n_0}. \tag{2}
\]

The field is then represented as a sum of the scattered field, \( E_{sc}(x, z) \) and the incident field, \( E_{inc}(x, z=0) \), where the incident field is the solution to the homogeneous wave equation. In this weak-scattering limit, the total field on the right hand side of Eq. (1) can be replaced with the incident field; the wave equation then simplifies to

\[
\left( \nabla^2 + k_0^2 n_0^2 \right) E_{sc}(x, z) = -2k_0^2 n_0 \delta n(x, z) E_{inc}(x, z). \tag{3}
\]

Chen and Stamnes have found from simulations that the Born approximation is valid over values of \( \delta n \) and radii of index structures, \( a \), for \( a\delta n \leq 0.08\lambda \) [25]. In this work, we use the Born approximation for all calculations and show through our experimental data that this approximation is valid for the range of index structures we measure.

In the forward scattering problem, the right hand side of Eq. (3) is a known quantity. Solutions to this differential equation show that the Fourier transform of the scattered electric field can be calculated from the convolution of the Fourier transform of the incident electric field and the Fourier transform of the index profile [26]:

\[
E_{sc}(k_x, L) = \frac{k_0^2 n_0}{k_z} E_{inc}(k_x, z = 0) \ast_{k_z} \left[ \delta n_{obj}(k_x, k_z - k_z) \right] \exp[-ik_z L], \tag{4}
\]

where \( E_{sc}(k_x, L) \) is the one dimensional Fourier transform of the scattered field measured at a distance, \( L \), from the object, \( E_{inc}(k_x, z = 0) \) is the one dimensional Fourier transform of the incident field, and \( k_x \) and \( k_z \) are the spatial frequency coordinates in Fourier space. The \( k_z \) values are defined in terms of the \( k_x \) coordinates and the spatial frequency of the incident wave, \( k_z \), such that \( k_z = (k^2 - k_x^2)^{1/2} \). The scattered field measurements are therefore taken on arcs of the \( k \)-sphere in Fourier space as shown in Fig. 1. These measurements of the scattered field at various incident angles are used to determine the Fourier transform of the index structure, which is then inverse Fourier transformed to find the index profile in real space.

Because this data is taken on an irregularly sampled grid, this inverse transform is accomplished using a discrete Fourier transform (DFT) as opposed to the more efficient fast Fourier transform (FFT). For a transform with \( N \) data points, a DFT requires \( N^2 \) computations while an FFT requires \( N\log N \) computations, so an FFT will be much faster. Another solution to this problem is interpolation onto a regular grid in the Fourier domain [27]. A more common method of solving the inverse problem is filtered backpropagation, using interpolation in real space, which is an extension of the filtered backprojection commonly used in computed tomography with x-rays [28]. Both methods were developed to speed up implementation of the backpropagation of scattered fields for large data arrays. As we will demonstrate in Sec. 4, small data arrays (~200 points) are sufficient for reconstruction, and so a DFT proves to be sufficiently fast for our calculations.
A representative application of optical diffraction tomography is imaging deeply-buried waveguides, which are small in their physical dimensions and amplitude. Therefore, the diffracted field is typically smaller than experimental noise sources such as optical scatter, which can be significant when the small sample is embedded in a thick volume. To overcome this difficulty, consider an array of equally-spaced, identical index perturbations, such as an array of parallel waveguides, that form a grating with a diffraction efficiency that grows as the square of the number of illuminated lines. The total index change of all the lines, \( \delta n_{\text{tot}} \), is the convolution of the index change of a single line, \( \delta n_{\text{obj}} \), with a comb spaced at the grating period, \( \Lambda \),

\[
\delta n_{\text{tot}}(x, z) = \delta n_{\text{obj}}(x, z) *_{x} \text{comb}(x),
\]

where \(*_{x}\) represents the one dimension convolution in \( x \). The \( \text{comb}(x) \) and its Fourier transform, \( \text{comb}(k_{x}) \) are defined as

\[
\text{comb}(x) = \sum_{m=-\infty}^{\infty} \delta(x - n\Lambda)
\]

\[
\frac{1}{\Lambda} \text{comb}(k_{x}) = \frac{1}{\Lambda} \sum_{m=-\infty}^{\infty} \delta(k_{x} - \frac{2\pi m}{\Lambda}).
\]

For real experiments, finite-sized beams are used, and in many experiments these have Gaussian profiles. The incident field and corresponding Fourier transform are then given by:

\[
E_{\text{inc}}(x) = A_{\text{inc}} \exp\left[-\left(\frac{x}{w}\right)^{2}\right],
\]

\[
E_{\text{inc}}(k_{x}) = A_{\text{inc}} \frac{w}{\sqrt{2}} \exp\left[-\left(k_{x} \frac{w}{2}\right)^{2}\right],
\]

where \( A_{\text{inc}} \) is the amplitude of the Gaussian field, and \( w \) is the \( 1/e \) electric field radius. Using the expressions for the Fourier transform of the index perturbation and field in Eq. (4), we find

\[
E_{\text{sc}}(k_{x}, L) = i \frac{k_{z}^{3} n_{0}}{k_{z}} A_{\text{inc}} \frac{w}{\sqrt{2}} \exp\left[-\left(k_{x} \frac{w}{2}\right)^{2}\right] *_{k_{x}} \left[ \delta n_{\text{obj}}(k_{x}, k_{z}, k) \text{comb}(k_{x}) \right] \exp(-ik_{z}L).
\]

This expression shows that in the far field, the diffracted electric field is given by the Fourier transform of a single index line sampled at a spatial frequency of one over the grating period.
The Gaussian incident field results in Gaussian shaped samples, or diffraction orders, in the far field, spaced at $2\pi/\Lambda$ in $k_x$ as seen from the result of the convolution integral:

$$E_{\text{inc}}(k_x, L) = i k_0^2 n_0 A_{\text{inc}} \frac{w}{k_z \sqrt{2}} A \exp\left[\frac{-i k_x L}{2}\right] \times \sum_{m=-\infty}^{\infty} \exp\left\{-\left[\left(k_x - \frac{2\pi m}{\Lambda}\right)^2 + \left(k_z - k\right)^2\right]\right\} \delta n_{\text{obj}}\left(\frac{2\pi m}{\Lambda}, k_z - k\right). \quad (9)$$

Because the power, and not the electric field, is measured at optical wavelengths, an expression for the Fourier transform of the index perturbation in terms of the power in each order of the diffraction grating is more useful. This is accomplished by taking the modulus square of Eq. (9) and then integrating over one grating period for each order of the diffraction grating. This gives an expression for the linear power in the $m^{th}$ order of the diffraction grating in terms of the Fourier transform of the index perturbation at the particular value of $k_x$ and $k_z$ corresponding to that order:

$$P^m = \frac{\left\{ m \frac{1}{2} \right\}^{2\pi \Lambda}}{2\pi} \left| E_{\text{inc}}(k_x, L) \right|^2 dk_x \approx \left( k_0^2 n_0 A_{\text{inc}} \frac{w}{k_z \sqrt{2}} \right)^2 \delta n_{\text{obj}}\left( m \frac{2\pi}{\Lambda}, k_z - k\right) \int_{-\infty}^{\infty} \exp\left\{-2\left[\left(k_x - \frac{2\pi m}{\Lambda}\right)^2 + \left(k_z - k\right)^2\right]\right\} dk_x. \quad (10)$$

As long as the Gaussian beams well separated, the integral over a single order can be approximated as an integral over $\infty$ with very little error. The linear power in the $m^{th}$ order is then given by:

$$p^m = \left( k_0^2 n_0 \frac{1}{k_z} \right)^{2\pi \Lambda} \left( \frac{A_{\text{inc}}}{2} \right)^2 \delta n_{\text{obj}}\left( m \frac{2\pi}{\Lambda}, k_z - k\right). \quad (11)$$

The linear incident power is given by $(A_{\text{inc}})^2 w \sqrt{\pi}/2$. Now the Fourier transform of the index perturbation at $k_z = 2\pi m/\Lambda$ and the corresponding $k_z$ value can be given in terms of the ratio of the scattered power measured in the far field and the incident power,

$$\delta n_{\text{obj}}\left( k_z = m \frac{2\pi}{\Lambda}, k_z - k\right) = \frac{k_z}{k_0 n_0} \frac{p^m}{p_{\text{inc}}} \Lambda \sqrt{\frac{p^m}{p_{\text{inc}}}}. \quad (12)$$

The Fourier transform of the index perturbation is now in terms of measurable quantities and can be calculated from power measurements of each order for a range of incident probe beam angles. The last step is to take an inverse Fourier transform, resulting in the quantitative, 2D cross section of the index perturbation.

The replication of the object results in a higher signal to noise ratio (SNR). The scattered field from each index line adds coherently, causing the peak intensity of the diffraction orders to grow as the square of the number of lines that are illuminated. While this does not increase the overall diffracted signal, the scattered signal is concentrated into a smaller area. By spatially filtering the signal so that only the diffracted order reaches the photodetector, uniform detected noise due to scatter is decreased, thus increasing the overall SNR. The width of the pinhole can be $2\pi/(2w)$, the width of the Fourier transform of the beam, while the samples are separated by $2\pi/\Lambda$. If the scatter noise is uniform, only $\Lambda/(2w)$ times the noise reaches the photodetector, while the entire signal is detected. This results in an increase of SNR of a factor of $(2w)/\Lambda$, or the number of lines of the grating that are illuminated by the
incident field. This can also be seen as decreasing the noise of the measurement system by averaging over many copies of the index perturbations in real space by recording only those Fourier components which correspond to the periodicity of the array. Since the peak intensity depends on the grating period for a fixed probe beam size, we can adapt to a wide variety of amplitudes of index changes by changing the period of the gratings.

The increased peak intensity at these discrete scattered orders comes at the expense of revealing only discrete samples of the object Fourier transform. As shown in Eq. (8), the convolution of the index structure in real space results in a sampling of the Fourier transform of the index perturbation. In the far field, the diffracted electric field is proportional to the Fourier transform of a single index line sampled at a spatial frequency, $d k_z = 2\pi /\Lambda$. The sampling of the Fourier transform defines the length, $L_x = 2\pi /d k_x = \Lambda$, in real space over which the index can be reconstructed. Therefore, the grating period is the maximum length in $x$ over which the index can be reconstructed. If the grating period is significantly larger than the size of the feature to be imaged, measurement of these discrete diffracted orders is sufficient to reconstruct the index of a single object.

Replication of the index structures to be measured allows imaging of very weak structures, but accurate measurements using optical diffraction tomography are still difficult to implement in practice due to the requirement of phase information on the scattered electric field. Since the phase of the electric field can not be directly measured at optical frequencies, some form of phase reconstruction is required. Phase reconstruction usually requires measurements of the intensity of the scattered field at multiple planes, at least one of which is in the near field, or prior information about the object [29]. There are also methods that use holography or interferometric methods to measure the phase directly [30, 31]. However, for index structures that are smoothly varying and symmetric, the Fourier transform of the perturbation is positive, real, and symmetric. Therefore, the diffracted electric field amplitude is given directly by the square root of the measured intensity and no phase reconstruction is necessary. This allows intensity measurements to be taken directly in the far field without a lens and does not require prior information about the index structure or interferometry.

3. Direct-write lithography

We use the direct-write lithography system described in [11] to write index structures in volume photopolymers using the perpendicular writing geometry shown in Fig. 2. For this system, as in many 3D lithography systems, the resulting index change will resemble the incident writing beam. Therefore, the index change created by dragging a Gaussian beam through the polymer will be symmetric and smoothly varying, thus fulfilling the requirements for optical diffraction tomography without phase reconstruction.

For all of the experiments described here, we use InPhase Technologies Tapestry™ HDS3000 media [1, 32], which is sensitive to green light. The 7.6 x 7.6 cm square samples consist of 1 mm of photopolymer sandwiched between two 1-mm thick glass plates.
frequency-doubled Nd:YAG laser at 532 nm is focused at a depth of 1.5 mm in the material with a 0.55 NA molded asphere corrected for spherical aberration due to 1.2 mm of glass. The system operates at 0.3 NA to avoid the need for active spherical aberration correction over the 1 mm polymer depth. We use high-precision stages to move the photopolymer in three dimensions. The diffraction gratings are optically ruled by focusing the green laser into the center of the photopolymer and translating the material in the y direction through the beam to draw a 5 mm line, with a constant change in index of refraction along y. A shutter is used to prevent the light from exposing the material in between the writing of each line. The writing powers for the data presented in this report range from 0.5–30 µW focused to a 0.75 µm 1/e² radius. The size of the beam at the focus is measured using a razor blade knife scan. The speed of the stages during the writing process is 2 mm/s.

4. Optical diffraction tomography: experiment and results

The gratings measured in this experiment consist of 142 lines spaced 35 µm apart or 71 lines spaced 70 µm apart. Both configurations form 5 x 5 mm diffraction gratings. Once the gratings have been written and cured, we use a collimated 532 nm laser beam approximately 2 mm in diameter to measure the diffraction efficiency of the grating. The index structures written in the photopolymer have significant structure in the z dimension, but are thin in the sense of Bragg diffraction and therefore the scattered intensity has many diffracted orders in the x dimension in the far field. Each grating is rotated about the y axis to measure the efficiency of the diffracted orders versus incident angle, as shown in Fig. 3. A beam block is used to block light from all other orders and any scattered light. A high dynamic range power meter and filters measure four orders of magnitude in intensity, which corresponds to 10 or 20 diffracted orders depending on the size of the index structure and the period of the grating. Because the index is real, its Fourier transform is symmetric, so we only need to take data for positive values of k_x and k_z. Data is also taken only in the far field without the use of a lens, avoiding traditional field-of-view constraints.

Fig. 3. Optical diffraction tomography experimental set up. Tomography measurements are taken after the samples are fully cured. A frequency-doubled Nd:YAG laser at 532 nm is used to probe the diffraction gratings. The sample is rotated to probe the grating at a variety of angles. Measurements are taken of each order at each angle with a high-dynamic-range power meter.

The diffraction efficiency data is processed using the method described in Sec. 2 and results in the reconstruction of the index of a single line in the x, z plane, as shown in Fig. 4. As expected, the cross section of the index qualitatively resembles the writing beam going through focus. Cross sections of this index are shown in Fig. 5. The cross section of δn in the x plane is taken at the center of the index in z, where z = 0. Similarly, the cross section of δn in the z plane is taken at x = 0. The ripples in the index reconstruction in x are caused by the finite sampling in Fourier space of the scattered field. For this data set, ten orders are measured for a grating with a period of 35 µm, corresponding to a maximum spatial frequency of k_x max = 1.8 µm⁻¹, which gives a minimum sinusoidal period of 3.5 µm in the reconstruction as seen in Fig. 5(a). The noise on the data has an amplitude of approximately 2 x 10⁻⁴. The
cross sections show that the index change in this photopolymer is not linearly proportional to the intensity of the focused writing beam, since the index shown is larger in scale than the $x, z$ cross section of the writing beam.

![Fig. 4](image1.png)

Fig. 4. Tomographic reconstruction of the cross section of the index of a single line of a diffraction grating written in photopolymer with the system shown in Fig. 2. The peak index change is $1.6 \times 10^{-3}$. Cross sections of the reconstructed index are shown in Fig. 5.

![Fig. 5](image2.png)

Fig. 5. Cross sections of the index change (shown in Fig. 4) written in the photopolymer in (a) $x$ and (b) $z$ at the peak of the index change. The cross section of $\delta n$ in the $x$ plane is taken at the center of the index in $z$, where $z = 0$. Similarly, the cross section of $\delta n$ in the $z$ plane is taken at $x = 0$. The small ripples of the index in the $x$ cross section are due to the finite range of spatial frequency data supplied to the tomographic reconstruction algorithm.

In addition to having a high enough density of samples in Fourier space, a large enough range of spatial frequencies is also necessary for accurate reconstructions of the index. The range of spatial frequencies determines the resolution of the reconstruction. This is tested by removing samples from the highest spatial frequencies in $k_x$ and $k_z$ and observing the change in the full width at half maximum (FWHM) of the resulting index structures in $x$ and $z$. As shown in Fig. 6, the FWHM’s in both $x$ and $z$ approach a constant value as the number of samples is increased. Therefore, adding more samples, i.e. covering a larger range of spatial frequencies, will not significantly change the reconstructed index. Consequently, the reconstructed images are not limited by the resolution of the measurement system.
Fig. 6. Full-width at half-maximum (FWHM) measurements of cross sections of the reconstructed index as a function of data points used in the reconstruction algorithm. The slopes of both curves are approaching zero, indicating that additional samples will not change the feature size significantly.

The algorithm used in these reconstructions is based on the Born approximation, and so it is also important to test whether the scattered field in this experiment obeys the Born approximation. An FFT beam propagation program simulates the forward scattering of a plane wave through the tomographic reconstruction of the index change without assuming the Born approximation. This tests the validity of the Born approximation for these experiments as well as testing for any errors in the reconstruction. The resulting calculated diffraction efficiency is shown in Fig. 7. The calculated efficiency is in good agreement with the experimental data, especially for the lower orders. To test the validity of the Born approximation, the efficiency is calculated for an index structure with a hundredfold lower amplitude. The resulting scattered field is multiplied by one hundred, and the intensity of this scattered field is compared with the experimental data. In this case, the agreement is much better for the higher orders. Scattering from weaker index structures would be closer in agreement with the Born approximation, but the error is still very small in our experiments. The FFT beam propagation simulation validates the magnitude and shape of the computed index as well as the use of the Born approximation for these index structures.

Fig. 7. Comparison of experimental diffraction efficiency and efficiency calculated from a fast-Fourier-transform beam-propagation method. There are no fit parameters used and so this calculation confirms both the shape and amplitude of the experimental reconstruction.

The tomographic image is also validated by comparing the reconstructed index with a qualitative image taken with a phase-shifted DIC microscope [33]. Because thin samples are ideal for imaging with DIC, the photopolymer sample is microtomed to a thickness of 10 μm. The sample is then covered with index matching fluid and a coverslip and imaged with a 10x, 0.3 NA objective [Fig. 8(a)] The phase-shifted DIC image does not directly show the index
profile, but is rather proportional to the change in the index profile along the $x$ direction. To compare more directly, the tomographic reconstruction of the index is differentiated along the $x$ direction and shown in Fig. 8(b). There is excellent agreement between the two images. There is also a much higher SNR for the tomography reconstruction due to the coherent addition of scattering from the individual index structures, giving a very clear image of the index change.

![Fig. 8. Comparison of (a) phase-shifted Differential Interference Contrast image and (b) $d/dx$ of an optical diffraction tomography reconstruction of a diffraction grating with a 35 $\mu$m period.](image)

5. Conclusions

We have demonstrated quantitative measurements of deeply buried index structures in photopolymers. Our method of replicating a single weak index structure produces high-precision reconstructions of features as small as 3 $\mu$m by 150 $\mu$m with an index sensitivity of $2 \times 10^{-4}$. The transverse feature sizes are on the limit of the resolution allowed in the derivation of the expression for the index change in terms of scattered fields due to the approximation that the index is changing slowly on the order of a wavelength. For greater resolution, a more rigorous derivation without this approximation is necessary. The ability to change the period of the gratings also allows us to image a wide variety of index change amplitudes with good SNR. We have shown that for the class of smoothly varying, symmetric objects, optical diffraction tomography can be performed with intensity-only measurements, significantly simplifying the experiment and data analysis. We have fabricated many copies of index structures with the appropriate symmetries, reconstructed the index, and validated the reconstruction. A FFT beam propagation simulation is used to verify both the accuracy of the reconstruction and to provide a quantitative measure of the accuracy of the Born approximation. These images of weak index structures are essential for a variety of volume fabricated index structures where traditional microscopy cannot provide high-resolution, quantitative phase images.

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